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**ULB**

# Uniprocessor Schedulability and Sensitivity Analysis of Multiple Criticality Tasks with Fixed-Priorities

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- Task models
  - Basic model
  - Multiple criticality model
- State of the Art
- Analysis of Vestal's algorithm
- Sensitivity analysis
- Conclusion

- Classical characteristics
  - Period:  $P_i$
  - Deadline:  $D_i$
  - Execution Time:  $C_i$
- $C_i$  is overestimated for critical tasks
  - → interference of critical tasks on non critical tasks are highly overestimated
  - → oversizing of the system

## Aeronautic standards: DO 178B

Level	Criticality	Failure condition	Description
A	5	Catastrophic	Failure may cause a crash
B	4	Hazardous	Failure has a large negative impact on safety of performance, or reduces the ability of the crew to operate the plane due to physical distress or a higher workload, or causes serious or fatal injuries among the passengers.
C	3	Major	Failure is significant, but has a lesser impact than a Hazardous failure (for example, leads to passenger discomfort rather than injuries)
D	2	Minor	Failure is noticeable, but has a lesser impact than a Major failure (for example, causing passenger inconvenience or a routine flight plan change)
E	1	No effect	Failure has no impact on safety, aircraft operation, or crew workload

- New model
  - Vestal: *"Preemptive scheduling of multi-criticality systems with varying degrees of execution time assurance"*
  - New notion: criticality level  $L_i$
  - One execution time per criticality level
    - Constraint:  $C_i(l-1) \leq C_i(l)$  for all  $l$
- Example
  - 2 criticality levels :  $\{1, 2\}$

Task	$D_i = T_i$	$L_i$	$C_i(1)$	$C_i(2)$
1	4	2	2	2
2	7	1	2	5

Task	$D_i = T_i$	Priority	$L_i$	$C_i(1)$	$C_i(2)$
1	4	High	2	2	2
2	7	Low	1	2	5

For task 2

For task 1

Task	$D_i = T_i$	Priority	$C_i$
1	4	High	2
2	7	Low	2

Task	$D_i = T_i$	Priority	$C_i$
1	4	High	2
2	7	Low	5

Why not just consider  $C_i(2)$  for all tasks?

Task	$D_i = T_i$	Priority	$C_i$
1	4	High	2
2	7	Low	5



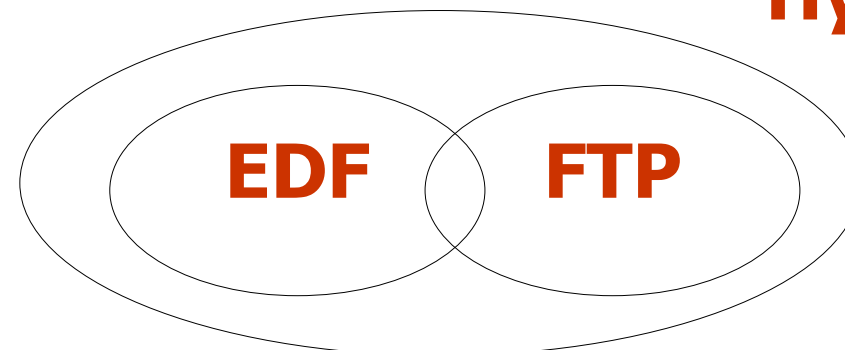
Not schedulable

**Constraint:  $C_i(l-1) \leq C_i(l)$  for all  $l$**

Task	$D_i = T_i$	Priority	$L_i$	$C_i(1)$	$C_i(2)$
1	4	High	2	2	2
2	7	Low	1	5	2

- Not schedulable if  $L_2=1$
- Schedulable if  $L_2=2$

- Vestal [2007]: *Preemptive scheduling of multi-criticality systems with varying degrees of execution times assurance*
  - Vestal's algorithm
- Vestal, Baruah [2008]: *Schedulability analysis of sporadic tasks with criticality specifications*
  - EDF and FTP are not comparable
  - Hybrid algorithm







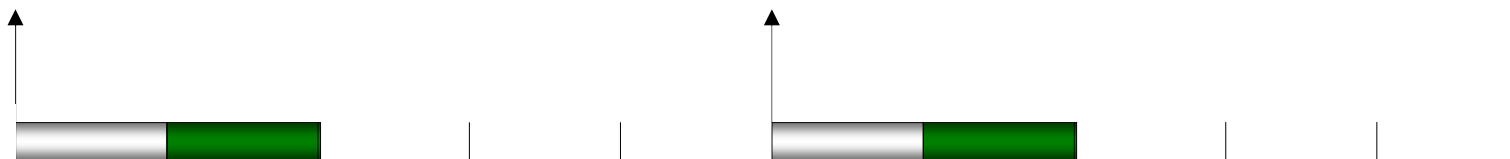
# Vestal's Algorithm

- 1) Using Audsley's algorithm
- 2) Using a tie breaker to choose the task to assign at a given priority level, based on critical scaling factor (Lehoczky 1989)

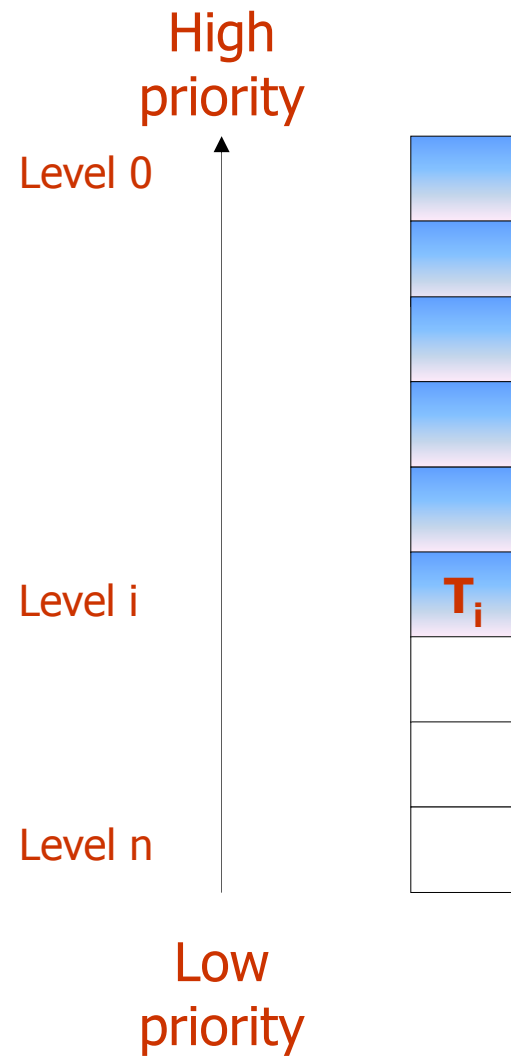
## Scaling factor

Maximum reduction factor which can be applied to the processor speed in such a way that the system is still schedulable

Task	Period	Deadline	Priority	Execution Time
	5	5	+	1 → 2.5
	5	5	-	1 → 2.5



# Scaling factor of a task



$\lambda_i =$  **Scaling Factor of  $T_i$  and higher priority tasks**

# Vestal's algorithm

Task	Pi	Di	Li	Ci(1)	Ci(2)	Priority
1	164	104	1	7	17	2
2	89	44	2	4	4	0
3	191	80	1	12	16	1
4	283	283	2	85	85	3

Priority \ Task	Task 1	Task 2	Task 3	Task 4
3	✘	✘	✘	1.69
2	3.87	1.19	3.47	
1		2.2	5	
0		11		

**Tie breaker: scaling factor**

- Audsley's algorithm is optimal
- Vestal's algorithm maximizes the scaling factor
  - Processor speed modulation
  - Reducing power consumption

Priority \ Task	Task 1	Task 2	Task 3	Task 4
3	✘	✘	✘	1.69
2	3.87	1.19	3.47	
1		2.2	5	
0		11		

➔ **Maximum scaling factor: 1.69**

High  
priority



Low  
priority

## Transformation

If the scaling factor of  $T_j$  at the priority level of the task  $T_i$  is greater than the one of  $T_i$ , then affecting the  $T_i$  priority to  $T_j$  can only increase the scaling factor of the task system.



The scaling factor is unchanged since task of lower priority do not affect these ones



The scaling factor is unchanged since it depends only of the set of higher priority task and not of their relative priorities



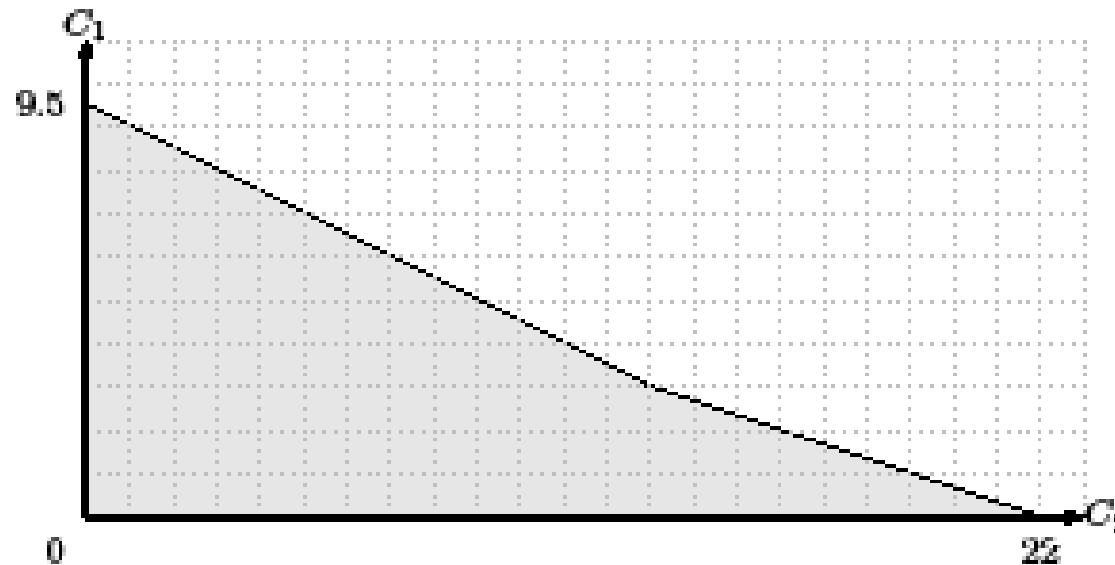
The schaling factor is increased since the priority of each task increased

# Sensitivity Analysis



- Aim : C-Space

Task	T <sub>i</sub>	D <sub>i</sub>
1	9.5	9.5
2	22	22



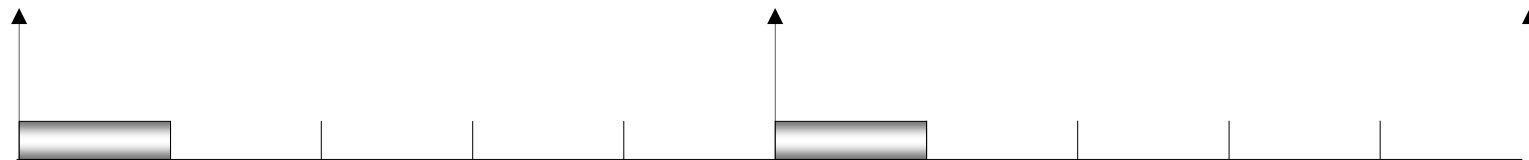
- Bini (*Sensitivity analysis for fixed-priority real-time systems*)
  - Perform a sensitivity analysis on the C-Space, in a given direction:
    - Subset of tasks
    - Ponderation
  - Particular cases
    - Scaling factor (all task with same ponderation)
    - One task (one task)

- Adaptation of the Bini's algorithm for multiple criticality tasks system
  - Idea: perform one sensitivity analysis per criticality level
- Example: sensitivity analysis on one task

# Sensitivity analysis on one task

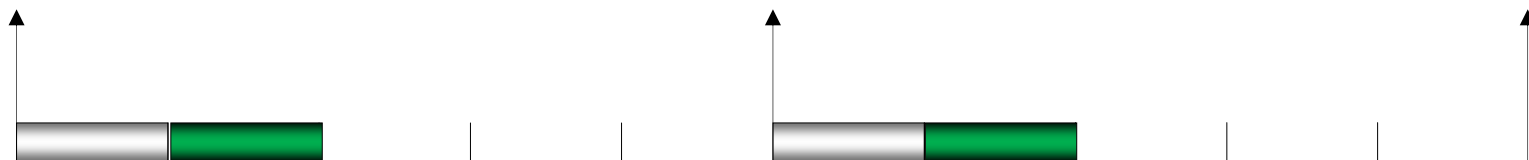
Task	Period	Deadline	Priority	Execution Time
	5	5	High	1
	5	5	Low	1

Grey task



$$\delta C_1 = 4$$



Green task



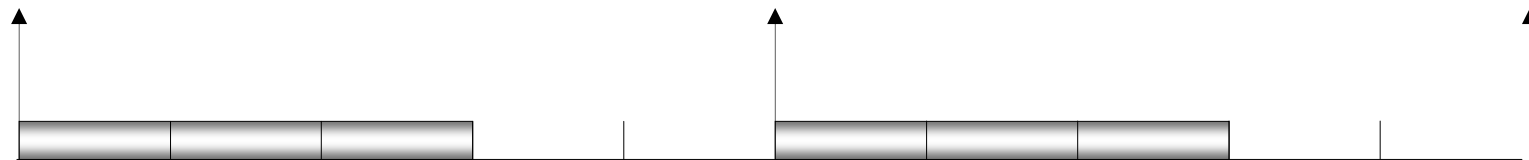
$$\delta C_1 = 3$$

$$\delta C_1 = \min(4, 3) = 3$$

# Sensitivity analysis on one task

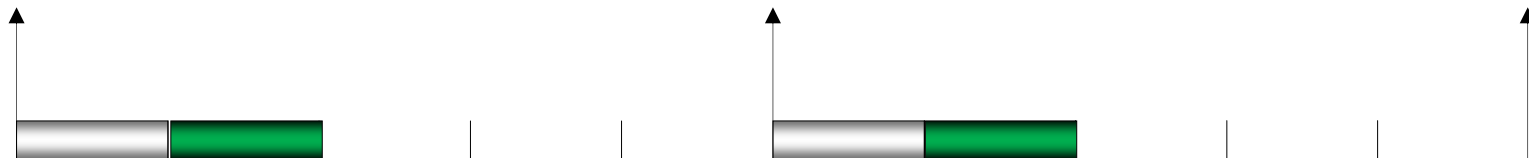
Task	Period	Deadline	Priority	Criticality	Execution Time 1	Execution Time 2
	5	5	High	2	1	3
	5	5	Low	1	1	1

Grey task



$$\delta C_1 = 2$$

Green task



$$\delta C_1 = 3$$

$$\delta C_1 = \min(2, 3) = 2$$



$$\delta C_1(1) = \min(3) = 3$$

$$\delta C_1(2) = \min(2) = 2$$

## Aim: sensitivity analysis on T2

Task	Ti	Di	Li	Ci(1)	Ci(2)
1	137	65	1	9	29
2	286	139	2	86	86
3	248	168	1	32	160

**Results:**

$$\delta C_2^{\max}(1) = 32$$

$$\delta C_2^{\max}(2) = 22$$

Task	Ti	Di	Li	Ci(1)	Ci(2)
1	137	65	1	9	29
2	286	139	2	108	108
3	248	168	1	32	160

**Need of a normalization step**

- Our works
  - Audsley's algorithm is optimal
  - Optimality property of Vestal's algorithm
  - Adaptation of sensitivity analysis of Bini
- Perspectives
  - Adapting our previous work to the multiple criticality model
    - Algorithm minimizing the number of processors (Dorin2008)
  - Sensitivity analysis